

# Guided Plasmon Modes of Elliptical Cross Section Silver Nanoridges

Zeyu Pan, *Student Member, IEEE*, Student Member, OSA, Junpeng Guo, Richard Soref, *Life Fellow, IEEE*, and Walter Buchwald

**Abstract**—Propagating two-dimensional plasmon polariton modes guided by elliptical cross section silver nanoridges are investigated in this paper. Mode field profiles, dispersion curves, propagation distances, and figure-of-merits of the plasmon modes are calculated for various elliptical cross section silver nanoridges. It is found that the elliptical cross section metal nanoridge, if designed properly, can support a tightly confined plasmon mode with a longer propagation distance and a higher figure-of-merit than the flat-top nanoridge waveguide of the same width. The optimal nanoridge waveguide is obtained when the elliptical waveguide cross section becomes a semicircular cross section. When the curvature of the elliptical nanoridge is large, the nanoridge plasmon mode approaches the wedge plasmon mode.

**Index Terms**—Optical waveguide, surface plasmon.

## I. INTRODUCTION

**S**URFACE plasmons are free electron density oscillations on the metal-dielectric interfaces, and can propagate along the metal-dielectric boundaries in the form of surface plasmon polariton waves with tightly confined sub-wavelength scale modes [1]–[3]. Surface plasmon modes in various waveguide structures, such as thin metal films [4]–[8], finite width thin film metal stripes and metal wires [9]–[17], trenches in the metal surface [18]–[29], metal dielectric layer structures [30]–[39], dielectric-loaded metal films [40]–[46] and metal wedges [25], [26], [47]–[52], have been extensively investigated. The quest for strong mode confinement and low propagation attenuation waveguides has motivated research efforts on various waveguide structures. Recently, 2-D surface plasmon waveguide modes of flat-top and triangular-shape silver metal nanoridges have been numerically investigated [53], [54]. Round-top gold nanoridge plasmon waveguides have been fabricated with the focused ion beam (FIB) milling technique [52].

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Z. Pan and J. Guo are with the Department of Electrical and Computer Engineering, University of Alabama, Huntsville, AL 35899 USA (e-mail: zp0002@uah.edu; guoj@uah.edu).

R. Soref is with the Department of Physics, University of Massachusetts, Boston, MA 02125 USA (e-mail: soref@rcn.com).

W. Buchwald is with the Solid State Scientific Corporation, Hollis, NH 03049 USA (e-mail: walter.buchwald@solidstatescientific.com).

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This paper presents comprehensive numerical investigations on the plasmon modes supported by elliptical cross section silver nanoridges. Mode field distributions, mode indices, dispersion curves, propagation distances, mode sizes, and the figure-of-merits of silver nanoridge plasmon waveguides with various surface curvatures are calculated. The motivation for investigating such elliptical cross section metal nanoridge waveguides is to find an optimal geometry that provides longer propagation distance and higher figure-of-merit. In addition, as will be shown, elliptical cross section nanoridge waveguides provide more uniform distributions of the plasmon mode fields when compared to the flat-top and wedge plasmon waveguides. This feature is important in applications requiring an expanded interaction region such as chemical and biological sensing. Elliptical cross section nanoridge plasmon waveguides can be fabricated with the focused ion beam (FIB) milling technique. FIB is a very powerful nanofabrication technique for realizing nanoscale structures and shapes in various materials [55].

## II. ELLIPTICAL CROSS SECTION SILVER NANORIDGE PLASMON WAVEGUIDES

The 3-D view and cross section of such an elliptical silver nanoridge waveguide are shown in Fig. 1(a) and (b), where the nano-scale metal ridge is extended in the  $z$ -direction with its width ( $w$ ) in the  $x$ -direction and the half ellipse height ( $h$ ) in the  $y$ -direction. The plasmon mode propagates along the ridge top in the  $z$ -direction. We assume the height of the ridge is sufficiently high that the substrate does not influence the ridge mode. The geometry of the elliptical cross section nanoridge is symmetric in  $x$ -axis, and non-symmetric in  $y$ -axis. Our previous work on the plasmon modes supported by the flat-top silver nanoridges [53] has found that a ridge width of 120 nm produces an optimal compromise between propagation distance and mode confinement. In this study, we thus fix the ridge width at 120 nm, for all elliptical cross section nanoridges investigated.

To describe the elliptical cross section, we use the curvature ( $\kappa$ ), instead of the height ( $h$ ). The curvature is the reciprocal of the radius of curvature ( $R$ ). The radius of curvature at the top of the ridge is  $R = w^2/4h$ . Thus, the curvature at the top of the ridge is  $\kappa = 1/R = 4h/w^2$ .

We use a full-vectorial finite-difference mode solver [56] developed by *Lumerical Solutions, Inc.* to calculate the 2-D plasmon modes of the nanoridge plasmon waveguides. The finite-difference method uses Yee's 2-D mesh with appropriate boundary conditions to numerically solve Maxwell's equations in the frequency domain. Solving the Maxwell equations becomes a problem of solving an eigenvalue problem. The mode index is obtained by solving the eigenvalue equation.

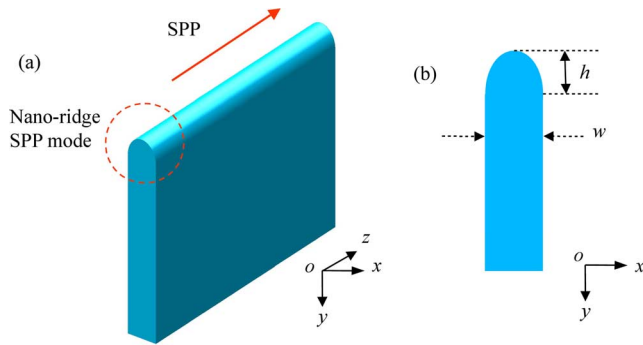


Fig. 1. (a) 3-D view of the elliptical nanoridge plasmon waveguide. (b) Cross section of the elliptical nanoridge plasmon waveguide.

We consider the situation where the surrounding medium of the nanoridges is air ( $\epsilon_d = 1.0$ ), and the nanoridges are made of silver with its electric permittivity  $\epsilon_m = -127.5 - 5.3j$  at the telecommunication wavelength of  $1.55 \mu\text{m}$  [57]. For the flat-top ridge with a width of  $120 \text{ nm}$ , the mode effective index and the attenuation coefficient are found to be  $n_{\text{eff}} = 1.018 - 0.00074j$  and  $261.87 \text{ dB/cm}$ , respectively. Although this study investigates silver as the ridge material, the analysis can obviously be extended to other types of metals and high electron density materials, such as heavily doped semiconductors [58]–[60] at different wavelengths.

We calculated the real and imaginary parts of the mode field components of the  $120 \text{ nm}$  wide elliptical silver nanoridge plasmon waveguide with  $\kappa = 16.67 \mu\text{m}^{-1}$  ( $h = 60 \text{ nm}$ ) at the  $1.55 \mu\text{m}$  wavelength. We found that the real parts of  $E_x$  and  $E_y$  are three orders of magnitude larger than the imaginary parts of  $E_x$  and  $E_y$ . The real parts of  $H_x$  and  $H_y$  are two orders of magnitude larger than the imaginary parts of  $H_x$  and  $H_y$ . But the real parts of  $E_z$  and  $H_z$  are two orders of magnitude less than the imaginary parts of  $E_z$  and  $H_z$ . So, we plot the real part of  $E_x$ , the real part of  $E_y$ , and the imaginary part of  $E_z$  mode profiles in the Fig. 2(a)–(c). Also, we plot the real part of  $H_x$ , the real part of  $H_y$ , and the imaginary part of  $H_z$  mode profiles in the Fig. 2(d)–(f). It can be seen that the  $E_y$  mode profile and  $H_x$  mode profile are symmetrical with respect to the center of the metal ridge (i.e.,  $x = 0$  plane), while the  $E_x$  and  $H_y$  profiles are anti-symmetrical with respect to the  $x = 0$  plane for such a plasmon mode propagating along the top surface of an elliptical metal ridge. The flat-top nanoridges ( $\kappa = 0 \mu\text{m}^{-1}$ ) have the similar symmetric properties with elliptical nanoridges [53]. The  $as_b^0$  mode and the  $ss_b^0$  mode of the finite width metal stripe in vacuum [10] can be considered as coupled two flat-top nanoridges located at the left and right sides of the finite width metal stripe.

We also calculated the field amplitudes of the three vectorial components of the  $120 \text{ nm}$  wide elliptical silver nanoridge plasmon waveguide with  $\kappa = 16.67 \mu\text{m}^{-1}$  ( $h = 60 \text{ nm}$ ) at the  $1.55 \mu\text{m}$  wavelength. Fig. 3(a)–(c) are the mode amplitude profiles of three electric field components ( $E_x, E_y, E_z$ ) at the  $1.55 \mu\text{m}$  wavelength. Fig. 3(d)–(f) are the mode amplitude profiles of three magnetic field components ( $H_x, H_y, H_z$ ) of the elliptical nanoridge waveguide at the same wavelength. It can be seen that the major components of the electric field are in

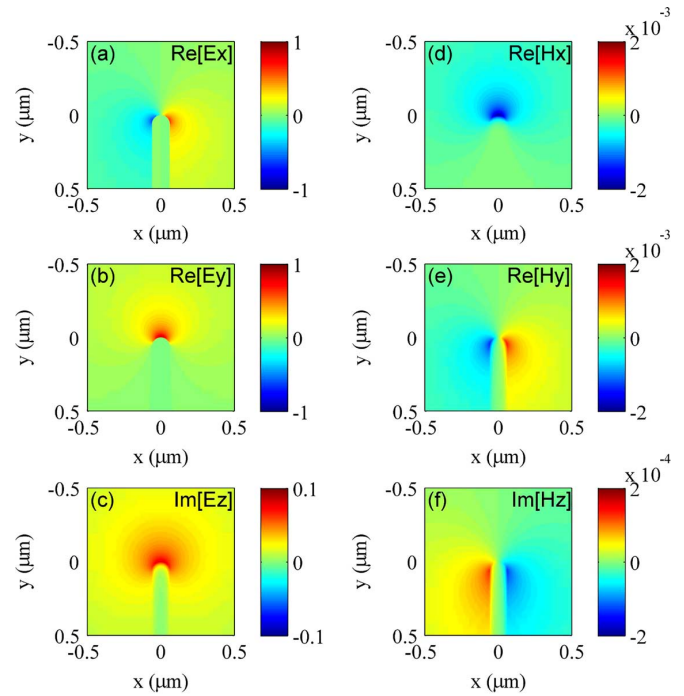


Fig. 2. Mode profiles at  $1.55 \mu\text{m}$  wavelength: (a) real part of the electric field  $E_x$ , (b) real part of the electric field  $E_y$ , (c) imaginary part of the electric field  $E_z$ , (d) real part of the magnetic field  $H_x$ , (e) real part of the magnetic field  $H_y$ , and (f) imaginary part of the magnetic field  $H_z$ .

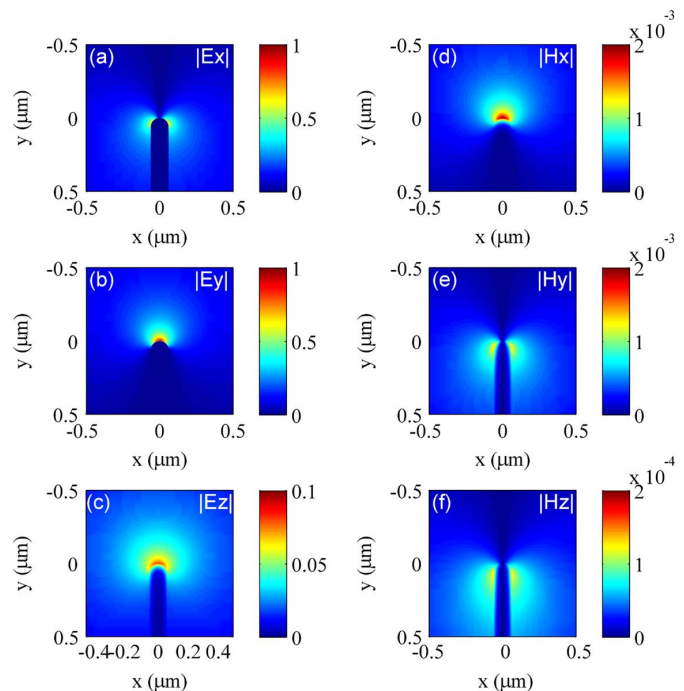


Fig. 3. (a)–(c) Electric field ( $E_x, E_y, E_z$ ) amplitude mode profiles of an elliptical silver nanoridge with  $\kappa = 16.67 \mu\text{m}^{-1}$  ( $h = 60 \text{ nm}$ ) at  $1.55 \mu\text{m}$  wavelength. (d)–(f) Magnetic field ( $H_x, H_y, H_z$ ) amplitude mode profiles of the silver nanoridge with  $\kappa = 16.67 \mu\text{m}^{-1}$  ( $h = 60 \text{ nm}$ ) at  $1.55 \mu\text{m}$  wavelength.

the transverse directions, which are about one order of magnitude larger than the longitudinal component of the electric field  $E_z$ . The major magnetic field components are also in the transverse directions, which are one order of magnitude larger than

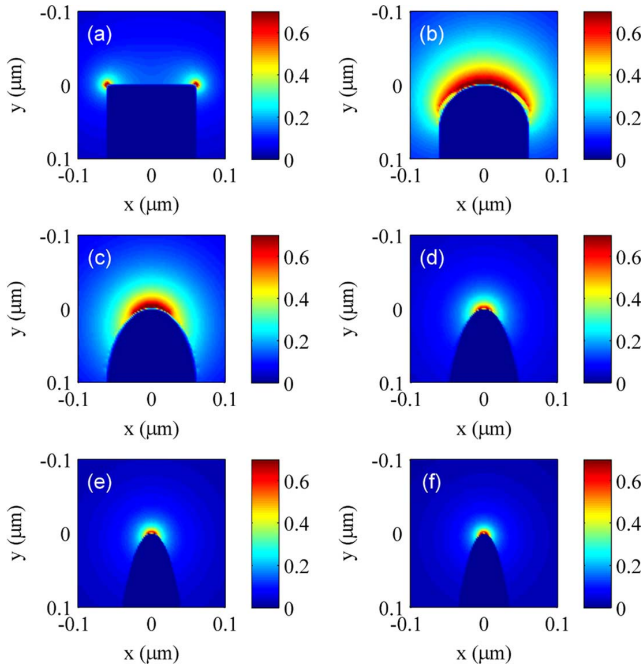


Fig. 4. Electric field intensity distributions of the 120 nm wide elliptical nanoridge plasmon waveguide with curvature equal to (a)  $0 \mu\text{m}^{-1}$ , (b)  $15 \mu\text{m}^{-1}$ , (c)  $30 \mu\text{m}^{-1}$ , (d)  $70 \mu\text{m}^{-1}$ , (e)  $110 \mu\text{m}^{-1}$ , and (f)  $150 \mu\text{m}^{-1}$  at  $1.55 \mu\text{m}$  wavelength.

the longitudinal component of the magnetic field  $H_z$ . Therefore, the elliptical cross section nanoridge plasmon mode can be considered as a quasi-transverse electromagnetic (TEM) mode.

We calculated the electric field intensity distributions of the fundamental plasmon propagating modes supported by elliptical nanoridges of different curvatures at the wavelength of  $1.55 \mu\text{m}$  with width of the nanoridges set to 120 nm in all cases. Fig. 4(a) shows that the electric field intensity distribution of the flat-top nanoridge has two hot spots located at each corner of the ridge, which can be considered as a hybrid mode of two  $90^\circ$  wedge plasmon modes first described in [53]. Fig. 4(b)–(f) shows the electric field intensity distributions of the elliptical nanoridge plasmon modes with the curvature of  $15 \mu\text{m}^{-1}$ ,  $30 \mu\text{m}^{-1}$ ,  $70 \mu\text{m}^{-1}$ ,  $110 \mu\text{m}^{-1}$ , and  $150 \mu\text{m}^{-1}$ , respectively. It can be seen that for the elliptical nanoridge with a curvature between 9 and  $18 \mu\text{m}^{-1}$ , the mode spans the entire ridge. As the curvature increases, the mode progressively converges towards the tip of the ellipse with increasing mode confinement. As the curvature increases to above  $18 \mu\text{m}^{-1}$ , the mode converges to only one hot spot at the top of the ridge, which can be considered as a small angle wedge mode. We also find that the mode energy is distributed over the entire ridge when the curvature is small. In this case, the elliptical nanoridge mode is seen to be insensitive to the change of curvature. However, once the curvature becomes greater than  $18 \mu\text{m}^{-1}$ , the mode is seen to be concentrated at the top of the elliptical ridge, and is seen to rapidly intensify with the increasing curvature. It also can be seen that the plasmon mode of the rounded finite width metal strip [13] can be considered as the coupled two elliptical nanoridge modes located at the left and right sides of the metal stripe.

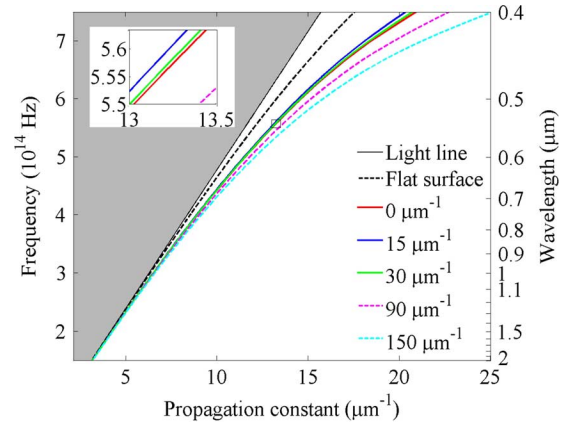


Fig. 5. Dispersion curves of the silver elliptical nanoridge plasmon waveguides of different curvatures and the comparison with the dispersion curve of the silver-air flat surface plasmon mode.

The mode dispersion curves of elliptical silver nanoridges of different curvatures are calculated and shown in Fig. 5. The black solid line is the light line in air. The black dashed line is the plasmon dispersion curve associated with the silver-air flat interface. In this figure, for all the curvatures, as the frequency increases, the plasmon mode dispersion curves drift away from the light line in air, suggesting slower group velocity and tighter mode confinement. This effect is far more pronounced for ridges with larger curvature. This is in contrast to the effects of the curvature on the dispersion curve, which is more easily seen in the inset of Fig. 5. Here, as the curvature increases from zero (i.e., the flat-top nanoridge), the dispersion curve first moves toward the light line (i.e., to the left side of the flat-top nanoridge dispersion curve in the inset), indicating a reduction in mode confinement. Once the curvature increases above  $16.67 \mu\text{m}^{-1}$ , the dispersion curve moves away from the light line and eventually falls in the right side of the zero curvature case, indicating the increase of both the mode confinement and propagation attenuation. The red line is the dispersion curve of the flat-top nanoridge waveguide. The blue line is the dispersion curve of the nanoridge waveguide with  $15 \mu\text{m}^{-1}$  curvature. The green line is the dispersion curve of the nanoridge waveguide with  $30 \mu\text{m}^{-1}$  curvature. The magenta and cyan dashed lines are the dispersion curves of the nanoridge waveguides with the curvature of  $90 \mu\text{m}^{-1}$  and  $150 \mu\text{m}^{-1}$ , respectively. It is also seen that the dispersion curves of ridges with curvatures between 9 and  $18 \mu\text{m}^{-1}$  are relatively insensitive to curvature changes. While beyond a curvature of  $18 \mu\text{m}^{-1}$ , the mode intensity is more concentrated to the tip of the elliptical ridge. The dispersion curve moves rapidly away from the light line when the curvature of the elliptical ridge continues to increase, and the ridge plasmon mode gradually approaches a wedge plasmon mode.

The real and imaginary parts of the elliptical nanoridge mode index versus the wavelength for several different curvatures ( $\kappa = 0 \mu\text{m}^{-1}$ ,  $15 \mu\text{m}^{-1}$ ,  $30 \mu\text{m}^{-1}$ ,  $90 \mu\text{m}^{-1}$ , and  $150 \mu\text{m}^{-1}$ ) are plotted in Fig. 6, where the black dashed lines are those of the silver-air flat plasmon mode. As the wavelength increases, both the real and imaginary parts of the elliptical nanoridge mode index decrease, indicating a reduction in the mode confinement as well as the propagation loss. We can also

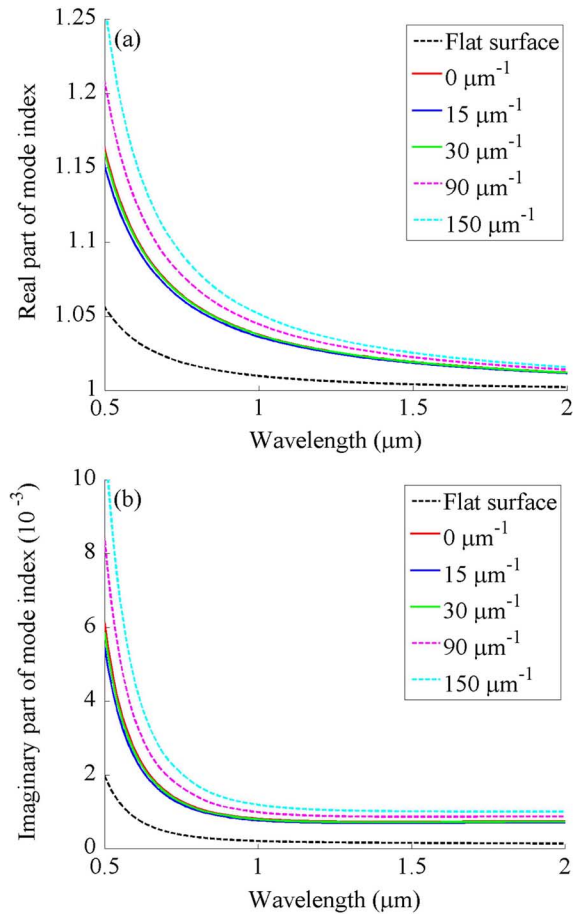


Fig. 6. (a) Real part and (b) imaginary part of the mode index versus the wavelength for different curvatures and the comparison with those of the silver-air flat plasmon mode index.

see when the curvature increases from the zero, both the real and imaginary part of the elliptical nanoridge mode index first reduce, and further increase of the curvature increases those of the elliptical nanoridge mode index, which is consistent with the results shown in Figs. 4 and 5.

The real and imaginary parts of the mode index versus the curvature at 1.55 μm wavelength are shown in Fig. 7. Interestingly, both the real and imaginary parts of the elliptical nanoridge mode index are first seen to decrease with an initial increase in the elliptical curvature, indicating a reduction in propagation attenuation and mode confinement, however, after reaching minimum values at 16.67 μm<sup>-1</sup>, rapid increase in both real and imaginary parts of the mode index is observed, which corresponds to a quick rise in both attenuation and confinement. It is interesting to note that considering the 120 nm ridge width here, a semi-circle of 60 nm radius would have a curvature of 16.67 μm<sup>-1</sup>. This suggests that a semicircular geometry is the optimal for reduced propagation loss and increased mode confinement.

In general, the propagation of surface plasmon modes can be characterized by a complex wave vector of the form  $\beta_z = n_{\text{eff}}k_0 = \beta - j\alpha$ , along the  $z$ -direction, where  $\beta$  is the phase propagation constant of the mode, and  $\alpha$  is the attenuation constant. The propagation distance is defined as the distance where the mode intensity attenuates to  $1/e$  of its initial value, i.e.,  $L_p = 1/(2\alpha)$ . The propagation distances are calculated

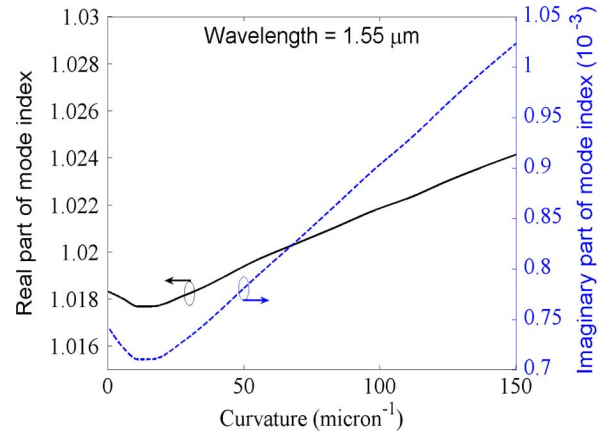


Fig. 7. Real and imaginary parts of the mode index versus the curvature at 1.55 μm wavelength.

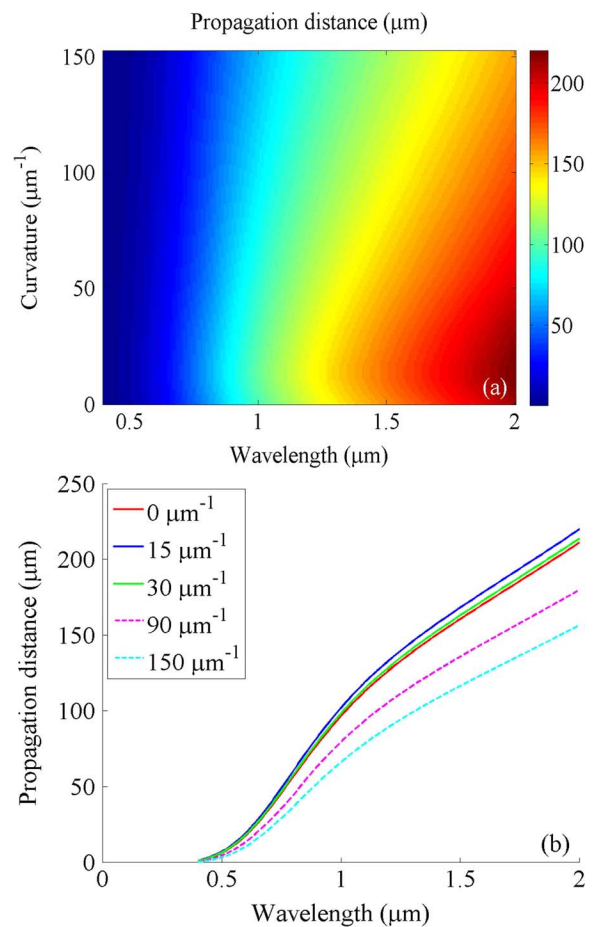


Fig. 8. (a) Propagation distance versus the wavelength and the curvature. (b) Propagation distance of the elliptical nanoridge mode versus the free space wavelength for different curvatures.

for the elliptical nanoridge plasmon waveguide at different curvatures and different free space wavelengths. The results are shown in Fig. 8(a) and (b). It can be seen that at any given wavelength as the curvature increases, the propagation distance first increases, and then reaches plateau for curvature between 9 and 18 μm<sup>-1</sup>, after which it is seen to decrease rather rapidly. As the wavelength increases, the propagation distance also increases. As discussed in the [26], for the wedge plasmon mode,

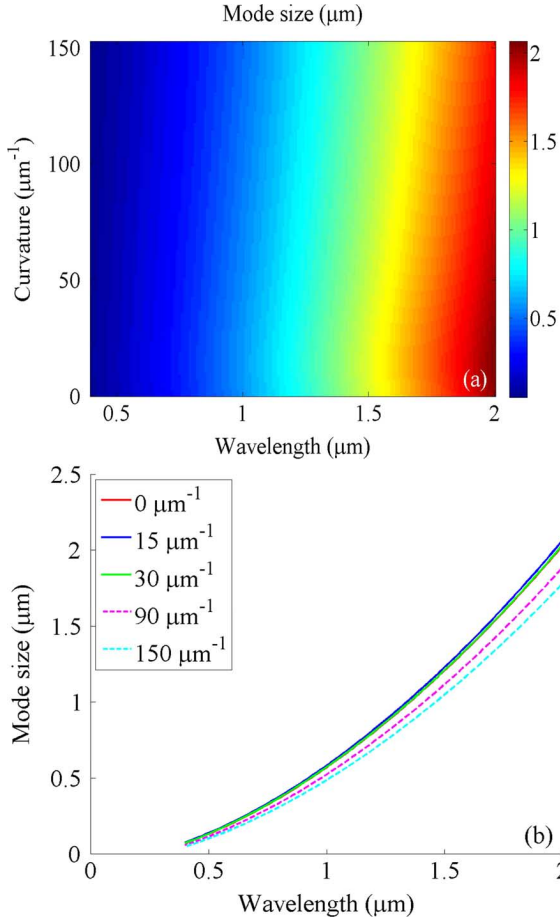


Fig. 9. (a) Mode size versus the wavelength and curvature. (b) Mode size of the elliptical nanoridge plasmon mode versus the free space wavelength for different curvatures.

the propagation loss increases dramatically as the wedge angle decreases. When the curvature is between 9 and  $18 \mu\text{m}^{-1}$ , it appears that the mode energy is distributed more evenly along the entire ridge, and the associated nanoridge plasmon mode can be considered as an infinite number of coupled large-angle wedge plasmon modes. Within this curvature range, these coupled wedge plasmon modes of the elliptical nanoridge have smaller loss, so the nanoridge plasmon mode has the longest propagation distance.

Outside the metal ridge in the surrounding dielectric medium, the transverse component of the complex wave vector is given by  $\beta_{\perp} = \gamma - j\delta$ , where  $\gamma$  and  $\delta$  describe the field oscillation and decay in the transverse direction, respectively. It follows from Maxwell's equations that the complex propagation constants in the propagation direction and the transverse directions are related as

$$(\beta - j\alpha)^2 + (\gamma - j\delta)^2 = \varepsilon_d k_0^2 \quad (1)$$

where  $k_0$  is the mode propagation constant in the free space, and  $\varepsilon_d$  is the dielectric constant of the surrounding dielectric. Solving (1), we can obtain  $\gamma$  and  $\delta$ , which are used to define the mode size as  $1/2\delta + 1/2\delta = 1/\delta$ . The mode size versus the free space wavelength and the elliptical curvature is shown in Fig. 9(a), while Fig. 9(b) shows the mode size versus the free

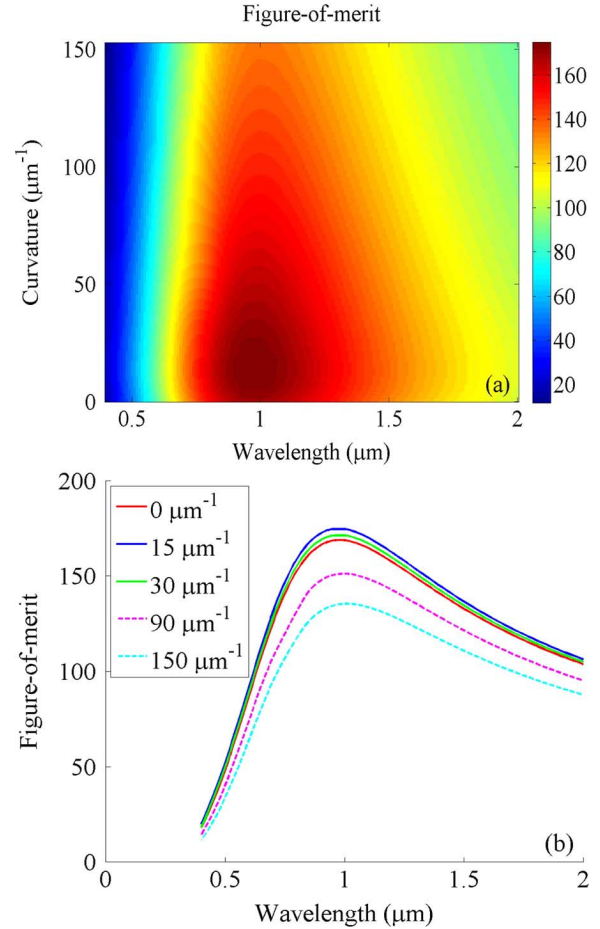


Fig. 10. (a) Figure-of-merit versus the wavelength and the curvature. (b) Figure-of-merit versus the wavelength for several curvatures.

space wavelength at various elliptical curvatures. Here it is seen that the mode size increases as the wavelength increases. Once again, for the curvature smaller than  $9 \mu\text{m}^{-1}$ , the mode size slightly increases, but when the curvature increases higher than  $18 \mu\text{m}^{-1}$ , the mode size decreases rapidly.

While it is always desirable to obtain surface plasmon waveguides with tight confinement and low attenuation, the reality is that there is always a trade-off between the propagation attenuation and the mode confinement [12], [61]. While tight mode confinement is the merit, attenuation is the cost. Figure-of-merits have been proposed to characterize this trade-off between attenuation and mode confinement [62], [63]. Here, we define the figure-of-merit of the nanoridge plasmon waveguide as the ratio of the propagation distance over the mode size:

$$\text{FoM} = (1/2\alpha)/(1/\delta) = \delta/2\alpha. \quad (2)$$

We calculated the figure-of-merit versus the wavelength and the curvature. The results are shown in Fig. 10(a). Fig. 10(b) shows the figure-of-merit versus the wavelength for several different curvatures. It can be seen from Fig. 10(a) and (b) that the figure-of-merit reaches a maximum at the  $1.05 \mu\text{m}$  wavelength for all curvatures considered in this study. It also can be seen that the magnitude of the figure-of-merit peak is related to the curvature, with values between 9 and  $18 \mu\text{m}^{-1}$  producing

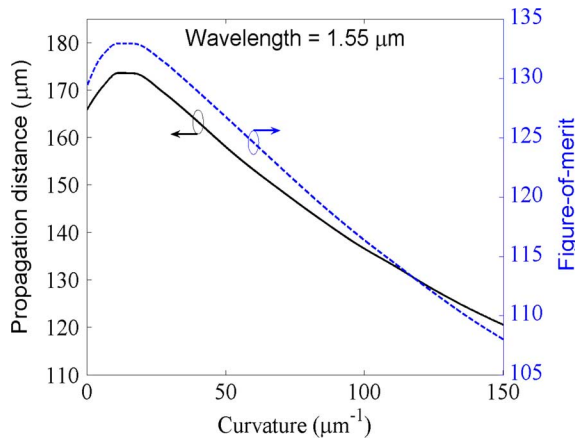


Fig. 11. Propagation distance and figure-of-merit of elliptical nanoridge waveguide mode versus the curvature at  $1.55 \mu\text{m}$  wavelength.

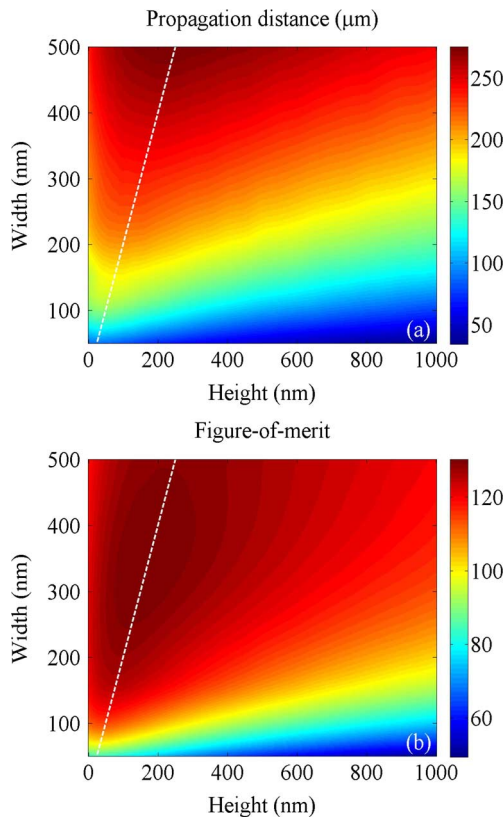


Fig. 12. Propagation distance and figure-of-merit versus the height and the width at  $1.55 \mu\text{m}$  wavelength.

figure-of-merits that are larger than those obtained for even the zero curvature (the flat-top nanoridge).

We specifically calculated the propagation distance and the figure-of-merit for the 120 nm wide elliptical nanoridge waveguide versus the curvature at the wavelength of  $1.55 \mu\text{m}$ . The results are shown in Fig. 11. As the curvature increases, both the propagation distance and the figure-of-merit increase when the curvature is less than  $9 \mu\text{m}^{-1}$ , and reach a plateau when the curvature is between  $9$  and  $18 \mu\text{m}^{-1}$ , after which both are seen to decrease dramatically. It is concluded that for the 120 nm wide elliptical cross section silver nanoridge waveguides discussed

here, the best performance can be obtained with a curvature between  $9$  and  $18 \mu\text{m}^{-1}$  at all wavelengths, with the ultimate performance being obtained when the excitation wavelength is roughly  $1.05 \mu\text{m}$ .

We also have calculated the propagation distance and the figure-of-merit for different elliptical height and nanoridge width at the  $1.55 \mu\text{m}$  wavelength. The results are shown in Fig. 12. The horizontal axis is the ellipse height of the nanoridge from  $0$  to  $1000$  nm. The vertical axis is the width of the nanoridge from  $50$  to  $500$  nm. It can be seen that as the height of the elliptical ridge increases, the propagation distance and the figure-of-merit increase first, and then decrease. The white dashed lines in the Fig. 12 indicate the elliptical cross sections which become semi-circles. The propagation distance and figure-of-merit reach the maximal values along this line. This is because the plasmon mode energy is more uniformly distributed over the entire ridge, when the cross section of the nanoridge waveguide becomes a semi-circle.

### III. CONCLUSION

Propagating plasmon modes supported by elliptical cross section silver nanoridges are investigated in this paper. We calculated the dispersion curves, propagation distances, mode sizes, and the figure-of-merits of these nanoridge plasmon modes. It is found that as the curvature of the elliptical nanoridge increases, both the propagation distance and the figure-of-merit first increase, reach a plateau, and then decrease dramatically. When the curvature falls between  $9$  and  $18 \mu\text{m}^{-1}$  for  $120$  nm wide silver elliptical ridges, the ridge plasmon modes have the longest propagation distance and the highest figure-of-merit. The elliptical nanoridge waveguides with the curvature between  $9$  and  $18 \mu\text{m}^{-1}$  have better performance in terms of the propagation distance and figure-of-merit than the flat-top nanoridge waveguides investigated previously [53]. It is found that the semi-circular cross section nanoridge waveguides, which give more uniformly mode energy distribution over the entire ridge surfaces, represent an optimal trade-off between mode confinement and propagation distance. The elliptical cross section nanoridge waveguides investigated in this paper are very desirable for applications that require large surface interaction area, such as in chemical and biological sensing.

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**Zeyu Pan** (S'12) received the B.S. degree in optical information science and technology from Nanjing University of Science and Technology, Nanjing, China, in 2010. He is currently working toward the M.S. degree at the University of Alabama, Huntsville.

His research interests include the nanoplasmonic waveguide, extraordinary optical transmission, nonlinear optics, and electromagnetic algorithms.

**Junpeng Guo** received the M.S. degree in nuclear plasma engineering and Ph.D. degree in electrical engineering from the University of Illinois at Urbana-Champaign.

He is currently an Associate Professor of electrical engineering and an Associate Professor of optical science and engineering with the University of Alabama, Huntsville. After his graduation from the Illinois, he became a Research Scientist with the former Rockwell Science Center, Thousand Oaks, CA, and later as a Member of Technical Staff with the Sandia National Laboratories, Albuquerque, NM. He has worked in numerous research areas in photonics, optics, and lasers. Most notably, he made the first thin-film micro-polarizer array for polarization imaging and 3-D displays. His current research interests are plasmonics, nanophotonics, and metamaterials.

**Richard Soref** (LF'03) received the Ph.D. degree in electrical engineering from Stanford University, Stanford, CA, in 1963.

He is currently a Research Professor at the University of Massachusetts at Boston. His research career in electrooptics spans 48 years.

Dr. Soref is a Fellow of the Optical Society of America, the Air Force Research Laboratory, and the Institute of Physics UK. In 2007, he received the Lifetime Achievement Award from the IEEE Photonics Society's International Conference on Group IV Photonics.

**Walter Buchwald** received the M.S. degree in physics, the M.S. degree in electrical engineering, and the Ph.D. degree.

He is currently the Director of Research for Solid State Scientific Corporation, Nashua, New Hampshire. He has held a variety of technical positions investigating semiconductor materials, devices, and advanced fabrication techniques at the Army Research Laboratory, the Raytheon Advanced Device Center, Axsun Technologies and most recently with the Air Force Research Laboratory where he initiated programs in plasmonics and IR integrated quantum optics. He has authored and coauthored over 90 publications and holds two patents and is a graduate faculty scholar with the Physics Department of the University of Central Florida.